CDS 130 Computing for Scientists

Topics:

MATLAB

1. Variables

- 1) Scalars, vectors, matrices.. can be assigned to a variable
- 2) Assignment
- 3) rules to name a variable:

À valid vairable name starts with a letter, followed by letters, digits, or underscores. You cannot define variables with the same name as Matlab key words such as for, end, if... Invalid variable names: 6x; end; n!; exp; ...

4) built-in variables

pi; i;

(note that the built-in variables can be reassinged with new values, e.g., pi = 4.0;)

Example: How to swap the values of two variables?

Matlabe code:

clear all; clc;

a = 3.0;

b = 4.5;

% To exchange the values of a and b, use a temporary variable to hold the value of the first variable.

c = a; a = b;

b = c;

2. Built-in math functions

Math operation order of precedence:

P. E.M.D. S. () ^ *, /, ∖, +, -

trigonomitircal functions: sin(x), cos(x), tan(x), asin(x), acos(x), sind(x), cosd(x), tand(x)

tansendental functions: $\log 10(x)$, $\log(x)$, $\exp(x)$:

powers: 3.0^4; sqrt(4.0); other functions: (please use matlab to find the answeers to the following functions). abs (-5); round(3.6) ceil (4.1); floor(4.0); mod(4.5); % finding the remainder of the interger division 4 devided by 5 rand(5); int16(3.6); int8(156); uint8(345); uint16(-1); char(128);

3. Anonymous functions. e.g., to create an anoymous function in matlab such that $f(x, y) = \sin^2(x) + \cos^2(y)$

matlab code: f=@(x,y) $(\sin(x))^2 + (\cos(y))^2$

4. User-defined functions.

Remember that the user-defined function must be saved with the same function name as the file name in the working directory.

For instance, to create $f(x, y) = \sin^2(x) + \cos^2(y)$ first, create (and save) a matlab script named 'my_func.m', second, in my_func.m, the script reads:

func f=my_func(x,y) f = $(\sin(x))^2 + (\cos(y))^2$ end

Having created this user-defined function my_func.m, you can use it just like other built-in math functions, such as:

a = my_func(3,4); b = my_func(4,5); ...

5. input and display

>> a = input('A variable is provided here = "); % matlab will wait for the user to provide a value after this command is executed.

>> display (a); % the content of a will be displayed

6. Create vectors : Row vector and Column vector

method 1: A(5) = 1; method 2: $A = \lfloor 2,3,4,5 \rfloor$; or $A = \lfloor 2; 3; 4; 5; \rfloor$ For row vectors, you can use either commas or spaces to separate the elements method 3: A = 2: -1: -6; (colon notation).

If the increment is 1, the short-handed notation is A = 2:5; (i.e., A = [2, 3, 4, 5]) method 4: form a new vector from previously defined vectors

>> A =
$$[1, 2, 3];$$

>> B = $[3, 4, 5];$
>> C = $[A, B]$

method 5: iterations

$$A(1) = 0;$$

for i = 2:6
$$A(i) = i$$

end

% this creates a new vector [0, 2, 3, 4, 5, 6], and it does so by appending new pieces onto an existing vector, one piece at a time.

method 6: A = rand(5) % this creats a vector with all element values between 0 and 1. method 7: A = linspace(0,2*pi, 10);

7. Vectors in a Matrix

- 1) row vector: A(5) means A(1, 5)
- 2) column vector A(5,1)
- 3) Transpose operator: A(5)' is now a column vector

8. Address vector elements

- 1) meaning of A(1,5) and A(5)
- 2) meaning of A(5,1)
- 3) A(1:3) is a new vector
- 4) A(0.2) is invalid; A(0) is also invalid

9. Vector operations

>> A =
$$[1, 2, 3]$$

>> B = $[3, 4, 5]$
>> C = A+B
C =
 $[4, 6, 8]$

4) Vector summation (sum of all vector elements)

- >> C = [4, 6, 8]; >> sum(C) ans = 20
- 5) Element-by-element operation (Attach . to the first vector) (extra credit) >> C = A. * B

>> C = A. * B
C =

$$[3, 8, 15]$$

>> C = $[1 \ 1 \ 1]$. / A;
C =
1 0.5 0.333333
>> C = $[1,2,3]$.^ 2
C =
1 4 9

6) Transpose operation

>> A = rand(5) % this creates a 5x5 random matrix >> B = A' % the transposed matrix is assigned to B now

10. Vector as a string

11. Create Matrices

method 1: A(4,5) = 0.0;method 2: A = [1, 2, 3; 3, 4, 5];method 3: >> B = [1:4];>> C = [4:7];>> A = [B; C];

method 4:

rand(10,8); % This creates a 10x8 matrix filled with random numbers [0,1]

zeros(10,8); % Create a 10x8 matrix filled will 0's. Ones(10,8); % Create a 10x8 matrix filled with 1's.

Example: How to create a 5x5 matrix with random numbers between -1 and 1?

A = rand(5) * 2 - 1;

12. Address matrix elements

A = rand(5,5)(1) A(5, 4) (2) A(1:2, [2,3]) (3) A([2,4,5], [1,3,4]) (4) A(:, 2:3) (5) A(:, :) (6) A(2, :)

13. Matrix Operations

(1) matrix added by a scalar >> A=[1, 2, 3; 3, 4, 5]; >> B = A + 2.0; B = 3 4 5 5 6 7

(2) matrix multiplied by a scalar
(3) matrix addition
(4) element-by-element operation (dot operator)
>> A = [1, 2, 3; 4, 5, 6];
>> A.*A
ans =
1 4 9
16 25 36

(5) Sum of matrix

....

(6) Mean and standard deviation of A >> mean(A) ans = >> std (A) and =

14. How to load data into Matlab

Save the file into the working directory of matlab, e.g. data.dat (alternatively, you can name it as data.mat). Now you can load the data using load data.dat

or (if it has the extension .mat). load data

15. How to check the size of a matrix?

A = rand(4,5);

To check the size, you have two commands to use:

>> whos A;

>> [M,N] = size(A); % In this case, M is the number of rows; and N is the number of columns

16. Iterations (for-loops)

(1) syntax: for i=1:10 do something

end

Example 1: A = [1, 3, 7]for myVar = A A = A + myVar; end

Example 2:

Considering the following iteration code, what is A(12)?

clear all; clc; A(9)=13;for i=[10:12]; A(i)=A(i-1)+37;end

Example 3:

using a for loop to calcualte $2^2+2^3+2^4+2^5+...+2^{20}$

Matlab code: clear all; clc; sum = 0; for i=2:20 sum= sum + 2^i; end sum

Example 4

using for loops to create the following vector: [1, 3, 4, 7, 11, 18, 29, 47, 76, 123, 199]

Matlab code:

clear all; clc; A(1) = 1; A(2) = 3; for i=3:11 A(i) = A(i-2) + A(i-1); end

17. Double nested for-loops

```
for i=1:100
for j =i:100
do something
end
end
```

Example (1): Using nested for-loops to create/modify matrix elements

```
11 12 13 14 15

13 14 15 16 17

15 16 17 18 19

Matlab code:

for i=1:3

for j = 1:5

A(i,j) = 8+i *2+j

end

end
```

Example (2): What does the following Matlab code generate?

```
clear all; clc;
for i=1:4
sum = 0;
for j = i:4
sum = sum + j;
A(i,j) = sum;
end
end
A
ans =
```

18. Colors

additive color model RGB [1,1,0]; [1,0,1]; [0 1, 1,], [0, 0, 0]

subtractive color model CYMK

RGB color model used in matlab:

Red=[1,0,0], % assign this color to variable Red a= [0.5, 0.5, 1]; % assign this color to variable a

19. Matrices as images:

Indexed images

How to create a image

(1) Create a colormap matrix: (the dimension is n x 3, n colors with each color represented by r, g, b components in 0-1).

(2) Create a matrix: M=rand(50); Designate/alter matrix elements

(3) imagesc(M) and/or imagesc

(4) coloarbar

Example: How to create a 6x6 black and white checkerboard?

Matlab code:

```
clear all; clc;
% create a color map with two colors
map = [0,0,0; 1, 1, 1];
% create an image matrix
for i=1:6
    for j= 1:6
        M(i,j) = mod (i+j, 2);
end
end
% display the image
image (M)
colormap (map)
```

20. Plot

Steps to make a plot: step 1: Guess the plot range, a, b. (-10, 10) step 2: create x and y vectors. Use x as an independent variable, and use y as a dependent vector: x = -10:0.01:10 $y = x.^3 - 1$ (note: dot operators) step 3: make a plot: plot(x, y) Example: Is the following Matlab statement correct or not?

plot([2,3,4, 5], [2,3,4,5], 'ok');

You can also plot multiple curves using plot. More advanced command of plot:

```
plot (x,y, '--gs', 'LineWidth', 2, 'MarkerSize',10, 'MarkerEdgeColor', 'b', 'MarkerFaceColor', [1.0,0.5,0.3]):
```

21. Write text in the graph

syntax:

text(x, y, 'text is here', 'FontSize', 14, 'Color', [0,10]);

22. Plot 2-D graphs:

understand the meanings of:

figure % generate a new figure;

hold on % the plot will be held in place

hold off % the plot will be erased;

shg % bring the figure to front; axis square % make a square figure axis equal % the units used in the x axis and y axis are equal axis off % the axes will not be displayed xlabel('string') ylabel('string') axis ([xmin, xmax, ymin, ymax]) print -dpng 'filename.png' drawnow % the plot will be drawn as soon as this command is issued. pause(n) % pause temporairly stops matlab execution for n seconds before continuing.

Example:

x = linspace(0, 2*pi, 100); y = sin(x): plot(x,y, '-o'): axis([0, 2*pi,-1.5,1.5])

Example 2: How to draw a circle?

clear all; clc; theta = linspace(0, 2*pi, 1000); r = 1.0; x = r* cos(theta); y = r* sin(theta); plot (x,y, '--b', 'MarkerSize', 16); axis off axis square print -dpng 'circle.png'

23. Fill

Use 'fill' to generate polygons filled with colors. fill (x, y, 'k')

Example:

 $\begin{aligned} x &= [0, 0, 1, 1]; \\ y &= [1, 2, 2, 1]; \\ c &= [1, 0, 0]; \\ \text{fill } (x, y, c); \\ \% \text{note: the coordinates of x and y must match. The ploting sequence of the points is important} \end{aligned}$

24. Relational operators

(1) Six relational operators: $>, <, >=, <=, ==, \sim=$

Example:

Given x = 4 and y = 2 these are some possible relational operations:

Operation:	Result:
k = x > y	k = 1
$k = x \le y$	k = o
$k = x \sim = y$	k = 1

25. Logic operators logic operators: &, |, Logic operators can be applied to vectors or matices.

Example1 : Given $\mathbf{x} = [7, 3, -0.5]$ and $\mathbf{y} = [0, 1, 3]$, these are some possible relational operations:

Operation:	Result:		
$\hat{\mathbf{k}} = \mathbf{x} \& \mathbf{y}$	k = [0, 1, 1]		
$\mathbf{k} = \mathbf{x} \mid \mathbf{y}$	k = [1, 1, 1]		

Example 2: Given arrays $\mathbf{x} = [0735]$ and $\mathbf{y} = [2870]$, these are some possible relational operations: **Operation: Result:**

operation.	neoun.			
k = x & y	k = [o	1	1	o]
$\mathbf{k} = \mathbf{x} \mid \mathbf{y}$	k = [1	1	1	1]
k = x & ~y	k = [0	0	0	1]

Example 3: M = [0.2, 0.3, 0.7; 0.6, 0.5, 0.5]; ~(M>0.5) ans:

[1, 1 0, 0, 1, 1]

26. Order of Precedence

(1) Parenthesis
(2) ~
(3) exp(), *, /, +, (4) Conditional operators, left to right (>=, >, <=, <, ==, ~=)
(5) &
(6) |

Example: Write a Matlab code to find the number of matrix elements greater than a threshold value.

```
\begin{split} M &= \operatorname{rand}(100);\\ \text{threshold} &= 0.25;\\ \text{counter} &= 0;\\ \text{for } i &= 1:100\\ & \text{for } j &= 1:100\\ & \text{if } M(i,j) > \text{threshold}\\ & \text{counter} &= \text{counter} + 1;\\ & \text{end}\\ & \text{end}\\ \text{end} \end{split}
```

```
28. While loop
while condition
do something
end
example:
a = 2;
b = 8
while a < b</li>
```

```
a = a + 2;
a
end
```

29. Numerical Integration

Example I: integrate the area enclosed by an irregular shape in an image.

(1) use imread (syntax) to load the sample. e.g.,

- M = imread('http://cds130.org/wiki/images/Area.jpg', 'jpg');
- (2) If the image is with the true-color type, convert it to the indexed image. new_M = rgb2ind(M, 2)

(note: the new matrix will only contain 0's and 1's. In other words, there are only two colors) (3) Check the type and size of the image.

 $[m,n] = size(new_M)$

(4) Access the matrix, and identify the areas of interest. (Calculate the total number of 1's and o's).

```
total_area = 0
black_area = 0
for i=0: length(new_M(:,1)) % alternatively you can use [m,n] = size(new_M) to find the
```

size

```
\label{eq:matrix} \begin{array}{ll} for j=0: length(new_M(1,:)) \\ total_area = total_area + 1; \\ if new_M(i,j) > 1 \\ & black_area = black_area + 1 \\ & end \\ & end \\ & end \\ & display('The fraction of the enclosed area is: '); \\ black_area/total_area; \end{array}
```

Example II. Area underneath a curve.

$$f(x) = x \sin(x^2) + x^2$$
 (0.2 < x < 1.3)

Step 1: plot the curve to get a feel of the problem.

```
x = -10:0.01:10;

y = x.*sin(x.^2) + x.^2;

plot(x,y)
```

Step: 2: discretize the range of x clear; dx = 0.01; xmin = 0.2; xmax = 1.3; Step 3: integrate the area.

area=0 % this needs to be initialized before you can use it.

```
for x=1: (xmax-xmin)/dx:xmax

b1 = x(i)*sin(x(i)^2)+x(i)^2;

b2 = x(i+1)*sin(x(i+1)^2)+x(i+1)^2;

trapezoid = 0.5 * (b1 + b2) * dx;

area = area + trapezoid;

end
```

Alternatively you can try this

Step 3: integrate the area.

area=0 % this needs to be initialized before you can use it.

```
for x=xmin: dx: (xmax-dx)

b1 = x*sin(x^2)+x^2;

x = x + dx;

b2 = x*sin(x^2)+x^2;

trapezoid = 0.5 * (b1 + b2) * dx;

area = area + trapezoid;

end
```

Step 4: print out the area that you have integrated.

display (area);

30. Population growth

Mathematical model:

$$\frac{d P}{d t} = \alpha P$$

Computational model:

P(i+1) = P(i) + dt * P(i) * rate; % rate = birth_rate - death_rate;

Note: the rate could be positive or negative. If rate > 0 (population growth), If rate <0, population decay.

Example: Currently you have \$1000 in a bank account. If the monthly interest rate is 10%,

24 months later, how much will you have in the same account?

% Step 1: initialization

birth_rate = 0.1; death_rate = 0; % you decide to use a vector to register the amount of money in each year. P(1) = 10000; % month 1.

% Step 2: iteration

for i=1:24 % 24 months $P(i+1) = P(i) * birth_rate + P(i);$ end

% Step 3: plot to see P(i) as function of month.

plot ([1:25], P); P(25)